

Here is a problem which is similar but less complex:
 Suppose we have three cardboard squares and we paint the edges red, blue or green respectively as shown in Fig. 4.
 Problem: Align the squares to form a 3×1 rectangle so that no two edges of like colour adjoin, and with three different colours on each long side.
 There are 768 possibilities, but the solution is not unique.
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 341. Dispersion of a wave packet

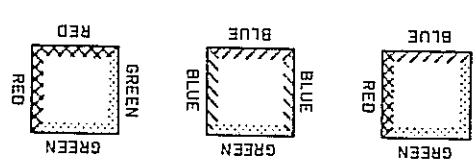


FIG. 4

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the same arrangement then applies to the integral to give the group velocity as in (6).

$$\gamma = \int_{-\infty}^{\infty} A(k) \sin 2\pi(kx - n(k)t) dk$$

represented by
in (4) would be replaced by integration. Hence the wave packet would be

If the number of sinusoidal components were infinite the summation in (5). The argument and the conclusion however remains unaltered.
we must replace the A in (4) by A , which will remain inside the summation

In the case where the sinusoidal components have unequal amplitudes for the sinusoidal components.

where the subscript 0 indicates evaluation at the average or 'peak' value
 $U = c_0 - \alpha_0^2 [dc/d\lambda]$

Substituting this into (6) we obtain Rayleigh's equation

$$\text{and since } k = 1/\lambda \text{ we have that } kd(\cdot)/dk = 1/\lambda d\lambda/dk d(\cdot)/d\lambda$$

$$= -\lambda d(\cdot)/d\lambda.$$

$$\text{But } n(k) = c(k)k \text{ so } dn(k)/dk = d(c(k)k)/dk$$

$$= c(k) + k(dc/dk)$$

(6) $U = \{dn(k)/dk\}_{k=0}^{k_1}$
Therefore from (3) we have

velocity $n_1 k_1 = n_1$ thus we conclude that the group velocity is $U = n_1$.
these waves and hence their resultant, the wave packet, progresses with a
whose amplitudes are modulated by $A \cos \theta$ or $A \sin \theta$ respectively. All of
 $\sin 2\pi(k_1 x - n_1 k_1)$ or $\cos 2\pi(k_1 x - n_1 k_1)$

waves of the type
Thus we see that the resultant wave packet is represented as a sum of

$$\gamma = A \cos \theta \sum_i \sin 2\pi(k_i x - n_i k_i) + A \sin \theta \sum_i \cos 2\pi(k_i x - n_i k_i). \quad (5)$$

in the above sum. We then obtain
Let $\theta = 2\pi(n_1 k_1 - n_0) t$, which is independent of k_1 , and expand sine

$$\gamma = A \sum_i \sin 2\pi(k_i x - n_i k_i + (n_1 k_1 - n_0) t).$$

Since $n_i = n(k_i)$, if we substitute (2) into (4) we have

$$(4) \quad \gamma = \gamma_1 + \gamma_2 + \dots + \gamma_N = \sum_{i=1}^N A \sin 2\pi(k_i x - n_i t).$$

then the resultant wave packet will be represented by